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## **Robust Control of DC motor Using Fuzzy Sliding Mode Control and Genetic Algorithm**

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### **Abstract**

Wide amplitude, DC motor's speed and their facile control cause its great application in industries. Generally the DC motors gain speed by armature voltage control or field control. In this paper, by using a combination of Fuzzy Sliding Mode methods and Genetic Algorithms, we have tried to optimally control the inverted pendulum by nonlinear equations. The results of this simulation have been mentioned in the conclusion. It seems that the results be acceptable results.

**Keywords:** Nonlinear control, Optimal, classical PID controller, Genetic Algorithm

### **1. Introduction**

There are variety methods for DC motors control that are presented since now. The presented methods for DC motors control are divided generally in three groups. Classic methods such as PID and PI

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controllers [1,2]. Modern methods (adaptation-optimum...) [3, 4, 5] .Artificial methods such as neural networks and fuzzy [6, 7] Theory are the presented methods for DC motors speed control.

The design method in linear control comprise based on main application the wide span ' of frequency, linear controller has a weak application, because it can't compensate the nonlinear system effect completely.

## 2. Model of DC Motor

The direct current motors are different kinds and several methods are presented for controlling of their speed. In this essay DC motor was chosen for speed control and by controlling the supply voltage was controlled it in nominal less speed.

The electric circuit of the armature and the free body diagram of the rotor are shown in fig. 1

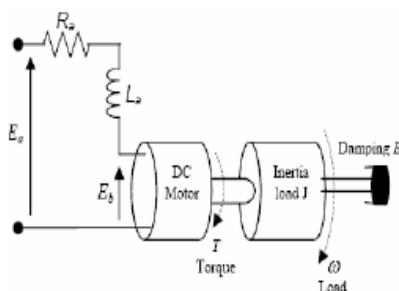


Figure 1: The structure of a DC motor

$$V_t = R_a I_a + L_a \frac{dI_a}{dt} + E_a \quad (1)$$

$$T = J \frac{d\omega}{dt} + B\omega - T_i \quad (2)$$

$$T = K_T I_a \quad (3)$$

$$E_a = K_a \omega \quad (4)$$

$$\frac{d\omega}{dt} = \varphi \quad (5)$$

With the following physical parameters:

$E_a$ : The input terminal voltage (source), (v);

$E_b$ : The back emf, (v);

$R_a$ : The armature resistance, (ohm);

$I_a$ : The armature current (Amp);

$L_a$ : The armature inductance, (H);

$J$ : The moment inertial of the motor rotor and load,(Kg.m<sup>2</sup>/s<sup>2</sup>);

$T$ : The motor torque, (Nm)

$\omega$  : The speed of the shaft and the load (angular velocity),(Rad/s);

$f$  : The shaft position, (Rad);

$B$ : The damping ratio of the mechanical system, (Nms);

$T_k$ : The torque factor constant, (Nm/Amp);

$B k$ : The motor constant ( $v\cdot s/rad$ ).

Block diagram of a DC motor is shown in fig. 2 [8].

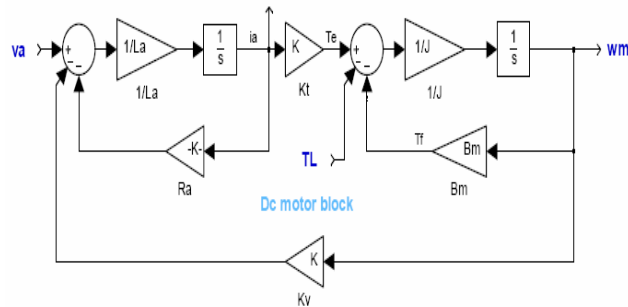


Figure 2.The block diagram of a DC motor

At first we control the DC motor by PID controller in fig.3

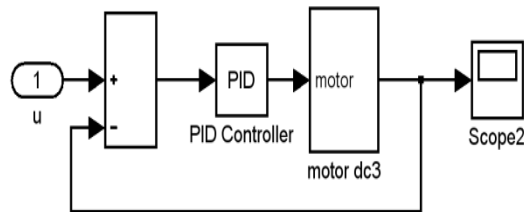


Figure 3.The block diagram of a PID controller dc motor

The results are based on fig.4

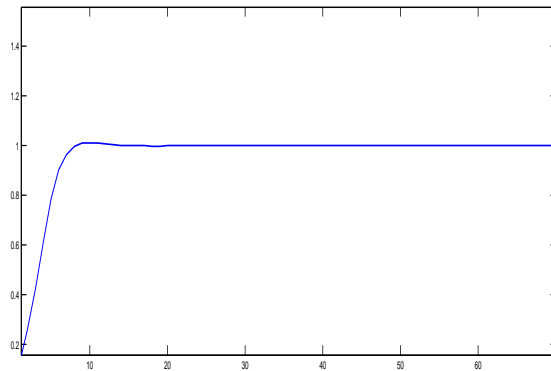


Figure 4.Simulated results PID controller of DC motor

The step response is proportionately a good response. Now with this controller we examine the step response of DC motor with uncertainly.(fig 5)

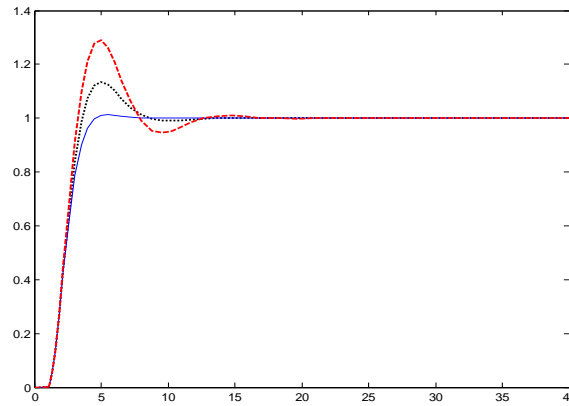


Figure 5. Simulated results PID controller of DC motor with uncertainties

You can see that the system's response to uncertain motor is not proper response.

### 3. Sliding Mode Controller

Nonlinear system control that its model isn't clear carefully works with tow methods:

- (1).Robust control methods.
- (2).Adaptive control methods.

In control view, uncertainly in modeling is divided in two main kinds:

- (1).Non certainly in existent Parameters in model
- (2).Estimating the lower step for system and being UN modeled dynamics in the estimating model.

Sliding control is one of the designed modes for robust control that make access to system desired application estimating system in model.

The major idea of this method is the controlling of nonlinear first grade system is easier than n grade system control in spite of uncertainly.

But this function maybe cause the control law with more energy that is not practicable implement station.

Sliding mode is really compromise between modeling and suitable operation with inaccurate design.

We consider the non linear system model in this rule:

$$X^n = f(x) + b(x)u \tag{6}$$

That F(x) is nonlinear function, its high boundary characterized as X function. B(x) is a continuous function that its high and low boundaries characterized by X function.

The good of finding X is in this way that in g(x) F(x) function we can follow the desirable mode in spite of uncertainly.

$$\tilde{X} = X - X_d = [\tilde{X}, \tilde{X}', \dots, \tilde{X}^{n-1}] \tag{7}$$

In ideal state

$$\tilde{X} = 0 \tag{8}$$

Sliding surface equation defines as below:

$$s = e' + \alpha_1 e + \alpha_2 \int e dt \tag{9}$$

Because of the signals of control that gain with this designing method has limited energy, it is necessary to:

$$X_d(0) = X(0) \tag{10}$$

In other word:

$$S(X, t) \equiv 0 \tag{11}$$

$$\frac{1}{2} \frac{dS^2}{dt} \leq -\eta|S| \tag{12}$$

In designing, the control law on S(t) continuously is noticed cause we should concentrate to carelessness in model in sliding surface and reduced the chattering effect.

We can write the system's dynamics when in some situation they are in sliding state.

$$S' = 0 \tag{13}$$

The gained control signals for this system are as below:

$$U = k_1 \times out_{fuzzy} * S \tag{14}$$

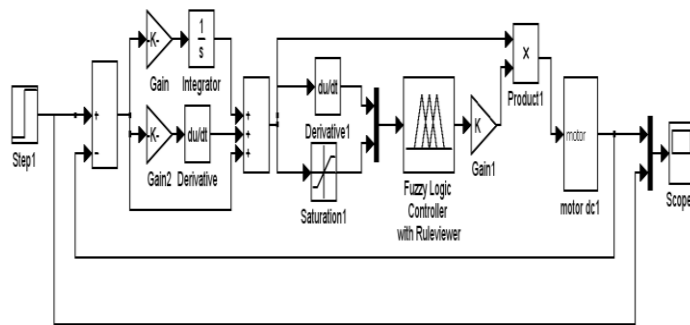


Figure6.simulink block diagram of FSMC

Fuzzy controls are designed based on created sliding surface and sliding surface changes. All of the fuzzy rules collection came in Table II

Table2. Fuzzy Rule

dS / S	NB	NS	ZE	PS	PB
N	B	B	M	S	B
Z	B	M	S	M	B
P	B	S	M	B	B

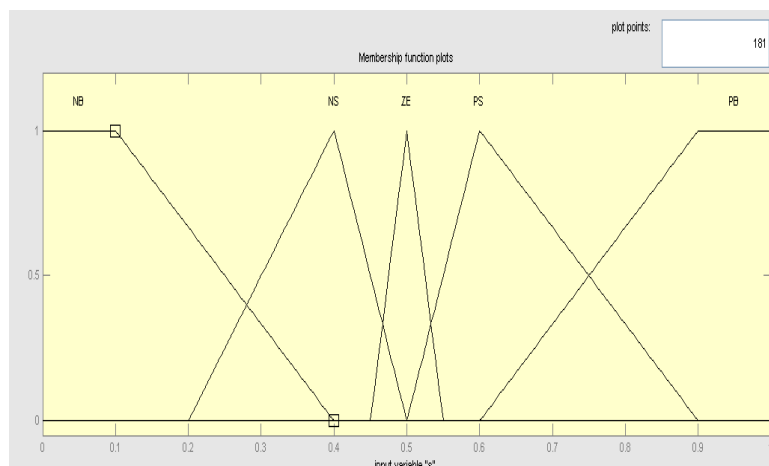
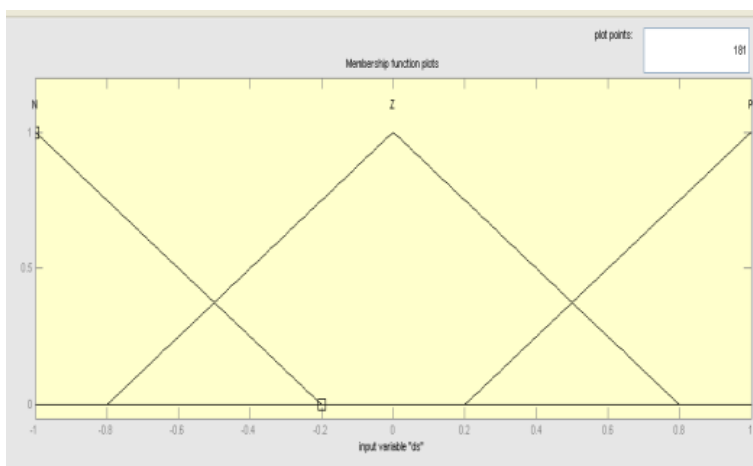


Figure 7.Membership functions for (ds/dt) normalized inputs

Figure 8.Membership functions for (ds/dt) normalized inputs

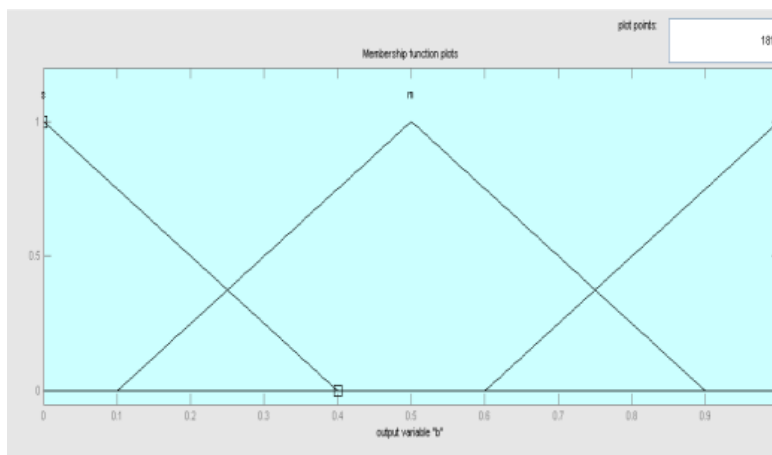


Figure 9.Membership functions for (out fuzzy) normalized outputs

### 5. Genetic Algorithm

Genetic algorithms are developed by Prof. Holland [5, 6]. This methodology is a derivative free optimization technique based on the concept of natural selection and evolution processes. The genetic operations are reproduction, crossover and mutation.

The evolution procedure of GAs is shown in Fig. 7. Producing initial populations is the first step of GAs. The population is composed of the chromosomes that are binary bit string or real codes. The

corresponding valuation of a population is called the “fitness function”. It is the performance index of a population. The fitness value is bigger, and the performance is better. The fitness function is defined as follow:

$$PI = \text{MIN} - \text{offset} - \sum |e| \tag{15}$$

Where “PI” is the fitness value, e is the speed error and “offset\_MIN” is a constant.

After the fitness function is calculated, the fitness value and the number of the generation determine whether the evolution procedure is stopped or not. In the following, the new populations are generated through reproduction, crossover and mutation. The selection operation decides which parents take part in reproducing offspring for the next generation. The crossover operation is applied to generate new chromosomes. The equations of the new populations generated from crossover are:

$$\begin{aligned} X_{01} &= (1 - \beta)X_{p1} + \beta X_{p2} \\ X_{02} &= \beta X_{p1} + (1 - \beta)X_{p2} \end{aligned} \tag{16}$$

Where xp1 and xp2 are the old chromosomes, β is the random value from 0 to 1, x01 and x02 are the new chromosomes. Mutation is a method to find the global optimal values. It changes the chromosomes from a random value.

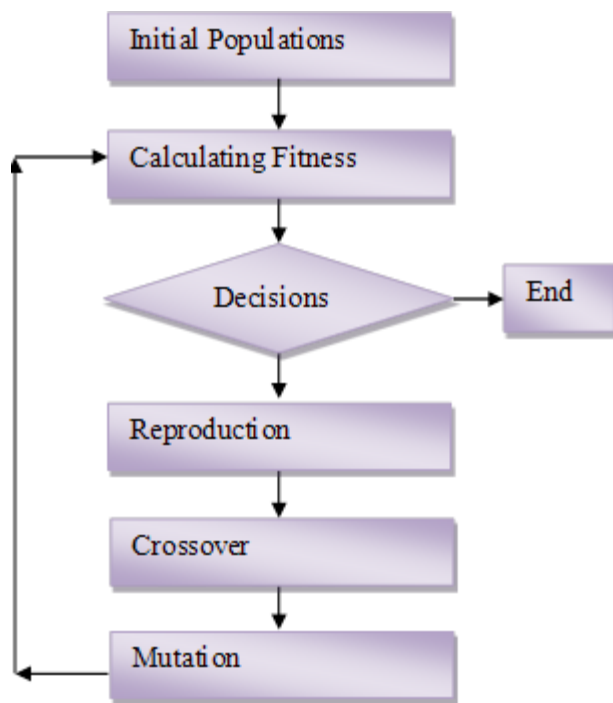


Figure 7.The evolution procedure of GAs

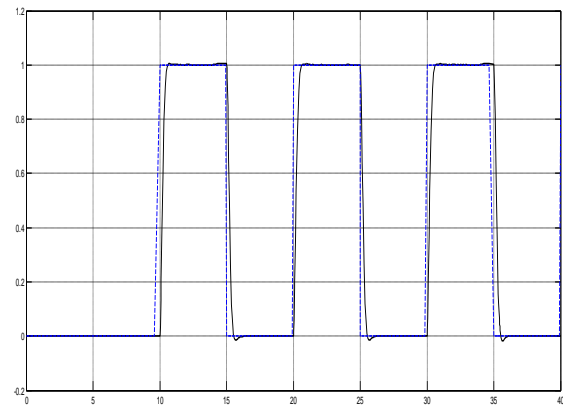


Figure 6.Simulated pulse results FSMC of DC motor

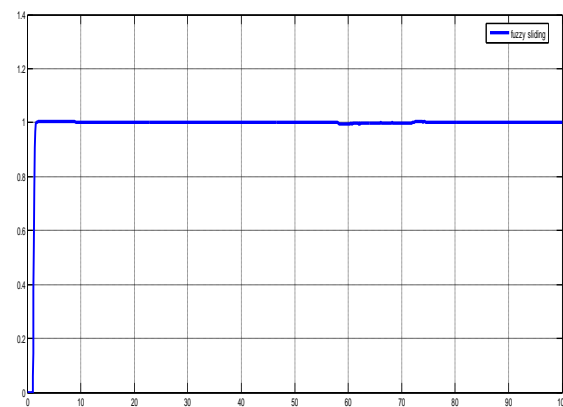


Figure 8.Simulated step results FSMC of DC motor

## 7. Conclusion

In this paper, a robust control system with the fuzzy sliding mode controller and the additional compensator is presented for a DC motor position control. According to the simulation results, the FSMC controllers can provide the properties of insensitivity and robustness to uncertainties and external disturbances, and response of the DC motor for FSMC controllers against uncertainties and external disturbance is the same Fuzzy sliding mode controller gives a better response to system than the fuzzy and classical PID controllers. If  $\alpha_1, \alpha_2, k_1$  control parameters set suitably

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